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Electronic and magnetic properties of 1T-TiSe₂ nanoribbons

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Abstract

Motivated by the recent synthesis of single layer $TiSe_2$, we used state-of-the-art density functional theory calculations, to investigate the structural and electronic properties of zigzag and armchair-edged nanoribbons (NRs) of this material. Our analysis reveals that, differing from ribbons of other ultra-thin materials such as graphene, $TiSe_2$ NRs have some distinctive properties. The electronic band gap of the NRs decreases exponentially with the width and vanishes for ribbons wider than 20 Å. For ultranarrow zigzag-edged NRs we find odd–even oscillations in the band gap width, although their band structures show similar features. Moreover, our detailed magnetic-ground-state analysis reveals that zigzag and armchair edged ribbons have non-magnetic ground states. Passivating the dangling bonds with hydrogen at the edges of the structures influences the band dispersion. Our results shed light on the characteristic properties of T phase NRs of similar crystal structures.

1. Introduction

Following the first experimental demonstration of graphene [1], two-dimensional (2D) materials have attracted increasing attention both experimentally and theoretically. Especially transition metal dichalcogenides (TMDs) [2-4] with chemical formula MX_2 (where M is a transition metal atom and X is a chalcogen atom) have been a favored subject. There are also other stoichiometric forms of TMDs such as titanium trisulfide (TiS₃) that can form monolayer crystals. [5] TMDs have a special 2D layered structure. Their mono- and few-layered forms offer many opportunities for fundamental and technological research [6-8] because of their exceptional electronic, mechanical and optical properties [9-12]. Furthermore, it is well known that various kinds of TMDs such as MoS₂, WS₂, MoSe₂, WSe₂, ReS₂, NbS₂, TiS₂, and TiSe₂ have been synthesized [2, 13-18] and studies have revealed that TMDs exhibit metallic, semimetallic, semiconducting, and even superconducting behavior with different phases such as 1 H, 1 T and their distorted forms.

The presence of exotic properties in 2D materials, that stemmed from increasing quantum confinement effects, has also motivated researchers to further reduce their dimension and to investigate onedimensional (1D) nanoribbons (NRs). In early studies it was shown that armchair and zigzag graphene nanoribbons (ZGNRs) were semiconductors with an energy gap decreasing with increasing ribbon width [19–22]. In addition, ZGNRs have ferromagnetically ordered edge states and can display half-metallic behavior when an external electric field is applied [23]. Furthermore, motivated by the potential use of single layer MoS₂ in nanoscale optoelectronic devices, its NRs have been studied intensively [24–26]. Armchair MoS₂ NRs are direct band gap semiconductors with a non-magnetic ground state. Unlike GNRs their band gaps do not vary significantly with the ribbon width [27]. However, zigzag MoS₂ NRs are ferromagnetic metals regardless of their width and thickness [28].

Despite the comprehensive research on graphene and single layer TMDs, studies on the electronic properties of the group IVB TMDs in the T phase, namely the 2D 1 T- MX_2 structures, are sparse. Nevertheless, 1 T-TiSe₂ [29–32] is an extensively studied quasi-2D TMD, which has a charge density wave (CDW) state and in condensed matter physics transitions from superconductivity to CDW phases has been shown to be very important [33, 34]. However, whether 1 T-TiSe₂ is a semimetal or a semiconductor is still an open question [35]. Since TiTe₂ is a semimetal with overlapping valence and conduction bands [36, 37] and TiS_2 is a semiconductor with an indirect gap [38, 39], it can be expected that the band gap of TiSe₂ is smaller or even non-existent. Note that in the periodic table selenium is in between sulfur and tellurium, and also selenium is less electronegative than sulfur. Therefore, both experimental and theoretical techniques have been used to identify the semiconducting or semimetallic nature of 1 T-TiSe₂ [40-43]. Very recently, Peng et al [44] grew TiSe2 ultrathin films on a graphitized SiC(0001) substrate by using molecular beam epitaxy (MBE). Their findings offer important insights into the nature of the CDW in TiSe2, and paved the way for potential applications based on its collective electronic states [44]. The successful MBE growth of TiSe₂ ultrathin films down to monolayer thickness motivated us to investigate 1D TiSe₂ NRs because of its interesting electronic and physical properties that are essentially related with its low dimensionality and effects due to quantum confinement. The main goal of this study is to find the characteristics of zigzag- and armchair-edged 1 T-TiSe2 NRs.

The paper is organized as follows. Details of the computational methodology are given in section 2. The calculated structural and electronic properties of single layer 1 T-TiSe₂ are described in section 3. Then we analyze 1 T-TiSe₂ NRs and present results from spin-unpolarized and spin-polarized calculations in detail in section 4. The last section, section 5, is devoted to the conclusion.

2. Computational methodology

The optimized structures and electronic properties of 1 T-TiSe₂ NRs with desired edges (zigzag or armchair) reported here are based on first-principle calculations within the density functional theory using the plane-wave projector-augmented wave method [45] implemented in the Vienna *ab initio* simulation package (VASP) [46–48]. The Perdew–Burke–Ernzerhof (PBE) [49] form of the generalized gradient approximation were adopted to describe the electron exchange and correlation for both spin-polarized and spin-unpolarized cases.

In order to correct the PBE band structure for a monolayer of TiSe₂, we also used the Heyd–Scuseria– Ernzerhof 06 (HSE06) functional [50, 51] which is known to give better electronic structure description that is close to experiments and produce accurate band gaps. Since it improves the accuracy of standard band gaps, we determined HSE06 functional parameters as an enhanced fraction of the Hartree-Fock exchange $\alpha = 0.25$ and screening 0.2 Å^{-1} . The kinetic energy cutoff for the plane-wave expansion was set to 500 eV where the Brillouin zone was sampled with Mon-khorst pack by $7 \times 1 \times 1$ k-point grids. For all band structure calculations, we used a $75 \times 1 \times 1$ Γ -centered k-point mesh. To avoid the interaction between periodic images, we ensured a sufficient large supercell which is 20 Å long perpendicular to the nanoribbon plane and with an edge-to-edge distance of at least 13 Å. At the same time, all the atoms in the supercell were fully relaxed during the geometry optimization. The convergence threshold for energy was chosen as 10^{-5} eV and 10^{-4} eV Å⁻¹ for the force. The charge distribution on the atoms were calculated by using the Bader analysis [52, 53].

Moreover, we investigated hydrogen saturated NRs in order to study the edge stability. The hydrogen saturation was realized by adding one hydrogen atom to the edge of Ti and Se atoms for the zigzag NRs, however for the armchair NRs one hydrogen atom was added to the edge of Se atoms and two hydrogen atoms are added to the Ti atom. For the determination of the most favorable structure which means the structure after hydrogenation, the binding energies were estimated from: $E_{\rm B} = E_{\rm T}[{\rm NR}] + {\rm n}E_{\rm T}[{\rm H}] - E_{\rm T}[{\rm NR} + {\rm n}{\rm H}]$, where $E_{\rm T}[{\rm NR}]$ is the total energy of the TiSe₂ nanoribbon, $E_{\rm T}[{\rm H}]$ is the total energy of the TiSe₂ nanoribbon saturated by hydrogen atoms, and n is the total number of saturated hydrogen atoms.

3. 2D monolayer TiSe₂

Before a comprehensive investigation of TiSe₂ NRs, we first present the atomic, electronic and magnetic properties of the TiSe₂ monolayer. Principally, layered structures of TMDs can form several different phases, e.g. H and T, that result in diverse electronic properties. Monolayer TiSe₂ has a hexagonal crystal structure composed of three atom layers with a metal atom Ti layer sandwiched between two chalcogen Se layers. Here octahedral coordination of the metal atoms results in the 1 T structure as shown in figure 1(a). Similar to graphite and graphene, in bulk TiSe₂ the monolayers are bound together through the interlayer van der Waals (vdW) interaction. The bond lengths are uniformly $d_{\text{Ti}-\text{Se}} = 2.56$ Å, $d_{\text{Se}-\text{Se}} = 3.72$ Å, where the angle between the Ti–Se bonds is $\theta_{Se-Ti-Se}$ $= 93.12^{\circ}$ and the optimized lattice constant is 3.52 Å from PBE calculation.

The PBE electronic band dispersion, shown in figure 1(b), shows that single layer TiSe_2 is a metal with a non-magnetic ground state. In addition, the partial density of states (PDOS) reveals that while there is negligible contribution from the Se orbitals around the Fermi level (E_F), those bands are mainly composed of Ti-3d orbitals (d_{z^2} , d_{xy} , d_{yz}). At the same time, a Bader analysis indicates that each Ti atom gives 1.4 electrons to the Se atoms which means that 0.7 electrons are taken by one Se atom, hence this situation shows that the character of the bonding is ionic. In contrast, the band structure of 1 T TiS₂ is semiconducting. Usually the difference in chalcogen atoms affects the structural properties, but has little influence on the electronic properties. For instance single layers of MoSe₂ and



 MoS_2 are both direct band gap semiconductors. However, a $TiSe_2$ sheet exhibits a metallic behavior with a low band crossing of the Fermi level, which is different from TiS_2 .

To further examine the electronic properties of 1 T-TiSe₂, we also calculated the band structure with the HSE06 method which is shown in figure 1(b). As can be seen the calculated bands below the Fermi level are shifted upward while above the Fermi level they are slightly shifted downward. At the same time, below the Fermi level the bands are decomposed but the bands above the Fermi level almost overlap with those of the PBE result. In general, relative to the experimental values, band gaps of semiconducting materials are underestimated by PBE. However, PBE+HSE06 provides better aggrement with the experimental values. Applying HSE06 corrections to metallic systems is not very common due to its computational cost, and no expected qualitative change in the band structures. Its effect is to introduce some shifts to the bands but the metallic character is preserved. For instance, singlelayered VS₂ and T-MoS₂ are still found metallic with HSE06 correction [54, 55]. Consequently, from both the PBE and HSE06 methods we may conclude that TiSe₂ is metallic.

4. NRs of 1 T-TiSe₂

4.1. Structural properties

The TiSe₂ NRs (TiSe₂-NRs) are obtained by cutting the 2D-TiSe₂ monolayer. According to the different directions of termination, there are two kinds of NRs: zigzag (TiSe₂-ZNR), and armchair (TiSe₂-ANR). Apart from the termination, TiSe₂-NRs are defined by their widths. The width of the zigzag NR is denoted as N_z (TiSe₂- N_z ZNR) and for armchair NR, the width is denoted by N_a (TiSe₂- N_a ANR). In figure 2 the lattice structure of TiSe₂-8ZNR and TiSe₂-5ANR are

presented. In our calculations, we consider width N_z from 2 to 10 and N_a from 2 to 8.

The fully optimized NRs exhibit structural deviation at the edges. For example TiSe2-ANRs are strongly distorted after relaxation, compared to TiSe2-ZNRs. In the triple layer networks, the edge selenium atoms shift their position from the Se layers to the Ti layer for both zigzag and armchair NRs whereas the Ti atoms at the edges shift their position from the Ti layer to the Se layers for only zigzag NRs. At one of the edges the Ti atom is closer to the lower Se layer, and the Ti atom at the other edge is closer to the upper Se layer. As seen in figure 2(b) for armchair NRs reconstruction takes place, as the Ti atoms at the edges moved towards the ribbon's center and the Se atoms tend to shift slightly outward. For TiSe₂-8ZNR, shown in figure 2(a), the Ti atoms moved slightly out of the plane, leading to a change of the Ti-Se bond length along the ribbon-axis. Nevertheless, the triple-layer networks are well kept intact for both ribbons. For instance, the average Ti-Se bond lengths for TiSe2-7ZNR are 2.56 Å in the inner site, and 2.44 Å at the two edges. The angle between Se–Ti–Se bond is 6.22° between the center and edge of the $N_{z} = 7$ zigzag NRs. For the TiSe₂-8ANR, coordination of atoms are different so that the Ti-Se bond length is different with values of 2.50, 2.57, and 2.64 Å in the inner site, at the edges it decreases to 2.38 Å. All of the NRs display the same structural property, and the only difference is that the bond lengths between the edge Ti-Se atoms are longer in ZNRs than those in ANRs. Similar to the case of MoS₂ NRs [28], at the edges the Ti-Se bond lengths decrease because of the irregular force on the edge atoms. Also, a Bader charge analysis tells us that charges on both Ti and Se atoms are equally distributed along the ribbon axis, since all of the Ti atoms lose the same amount of electron charge which is taken by the Se atoms. Likewise in the 2D-TiSe₂ layer,







every Ti atom loses 1.4 electrons to the Se atoms which gain 0.7 electrons along the ribbon axis.

4.2. Electronic properties

During the geometry optimization, we first carried out both spin-polarized and spin-unpolarized total energy calculations in order to determine the ground state of the different $TiSe_2 - N_z ZNR$ ($TiSe_2 - N_a ANR$). There is no energy difference between spin-polarized and spinunpolarized calculations which indicates that zigzag and armchair TiSe₂ NRs have a non-magnetic ground state. To be more confident about the magnetization of the edges, we also performed calculations for four different magnetic orderings for TiSe2-4ZNR and also TiSe₂-5ZNR by taking a double unitcell, such as antiferromagnetic (AFM), ferromagnetic (FM) (where, the atoms are located at different edges are AFM coupled, and at the same edge are FM coupled) (see figure 4(a)). We take the case of a TiSe₂-5ZNR as an example. Calculations starting from the four magnetic states, namely AFM-AFM, AFM-FM, FM-AFM, and FM-FM, and results in the same total energy. The same magnetic test is also applied to armchair NRs (see figure 4(b)). All the test results gave the same total energy and zero net magnetic moment. As a result, TiSe₂ armchair NRs have a non-magnetic ground state like MoS2-ANRs [28]. Thus, our calculation demonstrates that TiSe2-ZNRs and TiSe2-ANRs

are not magnetic and the edge states do not effect the magnetization of the structures.

After analyzing the structural and magnetic properties, we investigated the band dispersion of the TiSe₂-NRs. Electronic structures of TiSe₂-NRs show similar behavior like the single-layer 1 T-TiSe₂. In fact, we found that reducing the dimensionality from 2D to 1D, at a certain ribbon width a metal to semiconductor transition is found for both zigzag and armchair NRs as seen in figure 3. The band gap decays monotonically with the ribbon width for armchair NRs, however for zigzag NRs the rapid band gap decrease is superposed with an even-odd oscillation with increasing N_z and finally both structures switches to the zero energy gap of monolayer TiSe₂ (for $N_z \ge 7$, and $N_a \ge 6$). Similar oscillatory behavior is also observed in the equilibrium lattice constant for TiSe₂-N_zZNRs, when we increase the ribbon width N_z , the lattice constant approached slowly the value 3.52 Å which is the same as that calculated for the 2D-TiSe₂. The edge reconstructions are more effective in changing the equilibrium lattice constant of ultra narrow ribbons.

As illustrated in figure 3, the band gaps as a function of ribbon width for both zigzag and armchairedged NRs decay very rapidly, except for a small superposed oscillation observed in ultranarrow zigzag NRs. Similar band gap oscillations as a function of ribbon width were also predicted for other semiconducting NRs [23]. Nevertheless, due to the rapid decay in both



types of NRs, to provide a quantitative measure for these decays the band gap variations are fitted to the exponential functions, $E_{\text{gap}}(N) = \alpha \exp(-N\beta)$, where N is the width of the NR (for ZNRs $N = N_z$ and for ANRs $N = N_a$), and α and β are fitting parameters. For armchair and zigzag NRs, the values of the fitting parameters are found to be $\alpha = 5.06$, $\beta = 0.89$ eV and $\alpha = 6.17$, $\beta = 1.08$ eV, respectively. For $N \ge 7$, both types of NRs show metallic behavior.

Spin-unpolarized band structures of TiSe2-N_zZNRs are presented in figure 5. Notice that the band structures show similar property at the X-point for odd and even numbers of ribbon width. For the ribbon width of $N_z = 2$ a large gap of about 0.786 eV is found. Among the four ZNRs in figure 5, TiSe₂-4ZNR has the largest band gap of 0.201 eV, TiSe₂-3ZNR has a medium band gap of 0.165 eV, TiSe₂-5ZNR and TiSe₂-6ZNR have the smallest band gaps of 12 meV and 5 meV, respectively. Both the direct band gap of zigzag-edged and the indirect band gap of armchairedged ultranarrow NRs decrease with increasing ribbon width and eventually vanish for $N_z \ge 7$, and N_a \geq 6. The conduction band minimum (CBM) and the valance band maximum (VBM) cross resulting in a semimetallic band structure with overlapping bands.

In order to investigate this width-dependent transition in the band structure, as well as the odd–even variations observed in the narrowest ZNRs, we have considered partial charge density (PCD) profiles corresponding to VBM and CBM, or for some specific pair of points in the band structures. These pair of points are M1 and M2 for 2D-TiSe2 (figure 1), Z1 and Z2 for ZNRs, and A1 and A2 for ANRs (figure 5). The PCD plots of the VBM and the CBM as shown in figure 6 indicate the electronic states around the Fermi level. For TiSe2-3ZNR (TiSe2-4ZNR), the VBM and the CBM originate from a hybridized mixture of 3d electrons of Ti and 4p electrons of Se atoms with the hybridization being stronger in the VBM than that in the CBM. A comparison of the VBM states of TiSe2-3ZNR and TiSe₂-4ZNR indicate that they are localized more at the edges for odd N_z , whereas they are more uniform distributed for even N_z ribbons. For wider ribbons ($N_z > 4$), both the VBM and CBM states tend to delocalize and the metallic character is attained (this is evident for $N_z = 7$ and $N_z = 8$ in figure 6). With increasing N_z , the PCD plots at the Z1 and Z2 points tend to converge to those at the M1 and M2 pair for 2D-TiSe₂, where the corresponding states are localized on the Se and Ti atoms, respectively. The opening of a band gap in very narrow ribbons can be attributed to quantum size effects.

Typical band structures for a series of armchair TiSe₂ NRs are also shown in figure 5. Unlike zigzag NRs, the electronic structure of the armchair ribbons exhibit an indirect band gap for $N_a \leq 6$. The gap decreases exponentially with the ribbon width. The band gap is almost halved when the ribbon width is increased from $N_a = 2$ to $N_a = 4$. TiSe₂-5ANR still has a band gap of about 5.2 meV. Starting with $N_a = 6$, the











CBM dips into the Fermi level, so that the armchair NRs become metallic for wider widths. Some PCD plots for $TiSe_2-N_aANRs$ are also illustrated in figure 7. Similarly, the VBM and CBM states are composed of a hybridized mixture of Ti-3d and Se-4p orbitals for small NRs, however for the ribbon width larger than four, the hybridization becomes lost.

5. Hydrogen termination of edges

In order to investigate the effect of dangling states present at the edges of the NRs, we have passivated the edge atoms by hydrogen atoms. These unsaturated bonds influence the electronic properties of the ribbons. Naturally these states do not exist in the infinite $TiSe_2$ single layer, therefore reducing dimensionality from 2D to 1D it will be of importance control the dangling bonds. Earlier, it was shown for graphene NRs that when the dangling bonds at the edges are passivated with hydrogen atoms the electronic and magnetic properties of the ribbons are modified [22]. Unlike graphene, the TiSe₂-NRs have two types of atoms at the edges so that both Ti and Se atoms have to be passivated by hydrogen atoms to compensate the edge states.

Among possible configurations for the edge termination with hydrogen atoms, the most energetically favorable structure is shown for the $TiSe_2$ -4ZNR in figure 8. As seen in the figure where the edge atoms are passivated by hydrogen atoms symmetrically, hydrogenation of the NRs also enhances the stability of the structures. After hydrogenation the ground state energies is lowered, and the binding energy is found to be



11.7 eV for the case of TiSe₂-4ZNR. The band structures for several hydrogenated ZNRs are shown in figure 9. The TiSe₂- N_z ZNRs are all metallic except for $N_z = 4$.

We performed a analysis for the armchair NRs. In TiSe₂-3ANR, as an example shown in figure 8, the edge Se and Ti atoms are passivated by one and two hydrogen atoms, respectively. The binding energy of the TiSe₂-3ANR is 23.4 eV. After the hydogenation, TiSe₂-3ANR and TiSe₂-4ANR are semiconductors with an increasing band gap. Also, the VBM state moves a little away from the Γ -point in case of $N_a = 3$. TiSe₂-7ANR and TiSe₂-8ANR are still metallic after hydrogenation, however the overlap of the conduction and valance bands is reduced.

6. Conclusions

In this work, we have investigated the electronic and magnetic properties of zigzag and armchair-edged TiSe₂ NRs by means of first-principles calculations. Overall, our results demonstrate that these TMD NRs

which are in 1 T phase have quite different characteristics from NRs of other widely studied materials such as graphene or MoS₂. Our calculations revealed that only ultranarrow zigzag and armchair NRs exhibit semiconducting behavior and their band gap rapidly decreases to zero with increasing ribbon width. $N_a \ge 6$ and $N_z \ge 7$ NRs exhibit metallic behavior like 2D TiSe₂. The width dependency of the band gap can be fairly represented by an exponential decay function. Both zigzag and armchair ribbons have non-magnetic ground states. In addition, the robust metallic behavior of both zigzag and armchair TiSe2 NRs remains unaltered even after passivation of the edges by hydrogen atoms. The metallic character of the wider ribbons of TiSe₂ regardless of their edge symmetry is an advantageous property for utilizing them as 1D interconnects of nanoscale circuits.

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References

- Novoselov K S, Geim A K, Morozov S V, Jiang D, Zhang Y, Dubonos S V, Grigorieva I V and Firsov A A 2004 Science 306 666
- [2] Novoselov K S, Jiang D, Schedin F, Booth T J, Khotkevich V V, Morozov S V and Geim A K 2005 Proc. Natl Acad. Sci. USA 102 10451
- [3] Novoselov K S, Geim A K, Morozov S V, Jiang D, Katsnelson M I, Grigorieva I V, Dubonos S V and Firsov A A 2005 Nature 438 197
- [4] Coleman J N et al 2011 Science 331 568
- [5] Iyikanat F, Sahin H, Senger R T and Peeters F M 2015 J. Phys. Chem. C 119 10709
- [6] Wang Q H, Kalantar-Zadeh K, Kis A, Coleman J N and Strano M S 2012 Nat. Nanotechnology 7 699
- [7] Chhowalla M, Shin H S, Eda G, Li L-J, Loh K P and Zhang H 2013 Nat. Chem. 5 263
- [8] Huang X, Zeng Z and Zhang H 2013 Chem. Soc. Rev. 42 1934
- [9] Ataca C, Sahin H and Ciraci S 2012 J. Phys. Chem. C 116 8983
- [10] Wang H, Yu L, Lee Y-H, Shi Y, Chin M L, Li L-J, Dubey M, Kong J and Palacios T 2012 Nano Lett. 12 4674
- [11] Zhang Y J, Ye J T, Matsuhashi Y and Iwasa Y 2012 Nano Lett. 12 1136
- [12] Fang H, Chuang S, Chang T C, Takei K, Takahashi T and Javey A 2012 Nano Lett. 12 3788
- [13] Ross J S et al 2014 Nat. Nanotechnology 9 268
- [14] Tongay S, Zhou J, Ataca C, Lo K, Matthews T S, Li J, Grossman J C and Wu J 2012 *Nano Lett.* **12** 5576
- [15] Horzum S, Sahin H, Cahangirov S, Cudazzo P, Rubio A, Serin T and Peeters F M 2013 Phys. Rev. B 87 125415
- [16] Sahin H, Tongay S, Horzum S, Fan W, Zhou J, Li J, Wu J and Peeters F M 2013 Phys. Rev. B 87 165409
- [17] Tongay S et al 2014 Nat. Commun. 5 3252
- [18] Horzum S, Cakir D, Suh J, Tongay S, Huang Y-S, Ho C-H, Wu J, Sahin H and Peeters F M 2014 Phys. Rev. B 89 155433
- [19] Han M Y, Özyilmaz B, Zhang Y and Kim P 2007 Phys. Rev. Lett. 98 206805
- [20] Abanin D A, Lee P A and Levitov L S 2006 Phys. Rev. Lett. 96 176803
- [21] Sahin H, Ataca C and Ciraci S 2010 Phys. Rev. B 81 205417
- [22] Barone V, Hod O and Scuseria G E 2006 Nano Lett. 6 2748
- [23] Son Y-W, Cohen M L and Louie S G 2006 Nature 444 347
- [24] Li Q, Walter E C, van der Veer W E, Murray B J, Newberg J T, Bohannan E W, Switzer J A, Hemminger J C and Penner R M 2005 J. Phys. Chem. B 109 3169

- [25] Botello-Mendez A R, Lopez-Urías F, Terrones M and Terrones H 2009 Nanotechnology 20 325703
- [26] Pan H and Zhanga Y-W 2012 J. Mater. Chem. 22 7280
- [27] Ataca C, Sahin H, Aktürk E and Ciraci S 2011 J. Phys. Chem. C 115 3934
- [28] Li Y, Zhou Z, Zhang S and Chen Z 2008 J. Am. Chem. Soc. 130 16739
- [29] Salvo F D, Moncton D and Waszczak J 1976 Phys. Rev. B 14 4321
- [30] Fang C M, de Groot R A and Haas C 1997 *Phys. Rev.* B 8 4455[31] Li G, Hu W Z, Qian D, Hsieh D, Hasan M Z, Morosan E,
- Cava R J and Wang N L 2007 *Phys. Rev. Lett.* 99 027404
- [32] Kusmartseva A F, Sipos B, Berger H, Forro L and Tutis E 2009 Phys. Rev. Lett. 103 236401
- [33] Bovet M, Popović D, Clerc F, Koitzsch C, Probst U, Bucher E, Berger H, Naumović D and Aebi P 2004 Phys. Rev. B 69 125117
- [34] Morosan E, Zandbergen H W, Dennis B S, Bos J W G, Onose Y, Klimczuk T, Ramirez A P, Ong N P and Caval R J 2006 Nature Phys. 2 544
- [35] Rasch J C E, Stemmler T, Müller B, Dudy L and Manzke R 2008 Phys. Rev. Lett. 101 237602
- [36] de Boer D K G, van Bruggen C F, Bus G W, Coehoorn R, Haas C, Sawatzky G A, Myron H W, Norman D and Padmore H 1984 *Phys. Rev.* B 29 6797
- [37] Claessen R et al 1996 Phys. Rev. B 54 2453
- [38] Chen C H, Fabian W, Brown F C, Woo K C, Davies B, DeLong B and Thompson A H 1980 Phys. Rev. B 21 615
- [39] Samuelsen D, Pehlke E, Schattke W, Anderson O, Manzke R and Skibowski M 1992 Phys. Rev. Lett. 68 522
- [40] Pillo T, Hayoz J, Berger H, Levy F, Schlapbach L and Aebi P 2000 Phys. Rev. B 61 16213
- [41] Calandra M and Mauri F 2011 Phys. Rev. Lett. 106 196406
- [42] Hildebrand B, Didiot C, Novello A M, Monney G and Scarfato A 2014 Phys. Rev. Lett. 112 197001
- [43] Rösner M, Haas S and Wehling T O 2014 Phys. Rev. B 90 245105
- [44] Peng J-P, Guan J-Q, Zhang H-M and Song C-L 2015 Phys. Rev. B 91 12113
- [45] Blöchl P E 1994 *Phys. Rev.* B **50** 17953
- [46] Kresse G and Furthmüller J 1993 J. Phys. Rev. B 47 558
- [47] Kresse G and Furthmüller J 1996 Comput. Mater. Sci. 6 15 Kresse G and Furthmüller J 1996 Phys. Rev. B 54 11169
- [48] Kresse G and Joubert D 1999 Phys. Rev. B 59 1758
- [49] Perdew J P, Burke K and Ernzerhof M 1996 Phys. Rev. Lett. 77 3865
- [50] Heyd J, Scuseria G R and Ernzerhof M 2003 J. Chem. Phys. 118 8207
- [51] Heyd J, Scuseria G R and Ernzerhof M 2006 J. Chem. Phys. 124 219906
- [52] Bader R F W 1990 Atoms in Molecules—A Quantum Theory (Oxford: Oxford University Press)
- [53] Henkelman G, Arnaldsson A and Johnson H 2006 Comput. Mater. Sci. 36 354
- [54] Feng J, Sun X, Wu C, Peng L, Lin C, Hu S, Yang J and Xie Yi 2011 J. Am. Chem. Soc. 133 17832
- [55] Kan M, Wang J Y, Li X W, Zhang S H, Li Y W, Kawazoe Y, Sun Q and Jena P 2014 J. Phys. Chem. C 118 1515